

# Determination of Seismic Design Forces

Donald L. Anderson, P.Eng

Prof. Emeritus, UBC

The original Powerpoint presentation was prepared by

Jag Humar of Carleton University

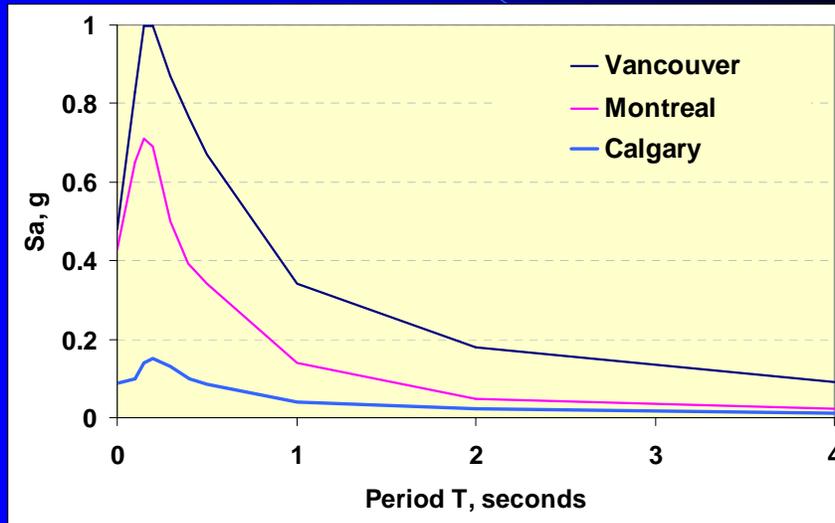
which is greatly appreciated.

December 2002

## Overview

- UHS spectrum
- Foundation factors
- Design spectrum
- Static load provisions
- Periods
- $M_v$  and J factors
- Torsion
- Dynamic analysis

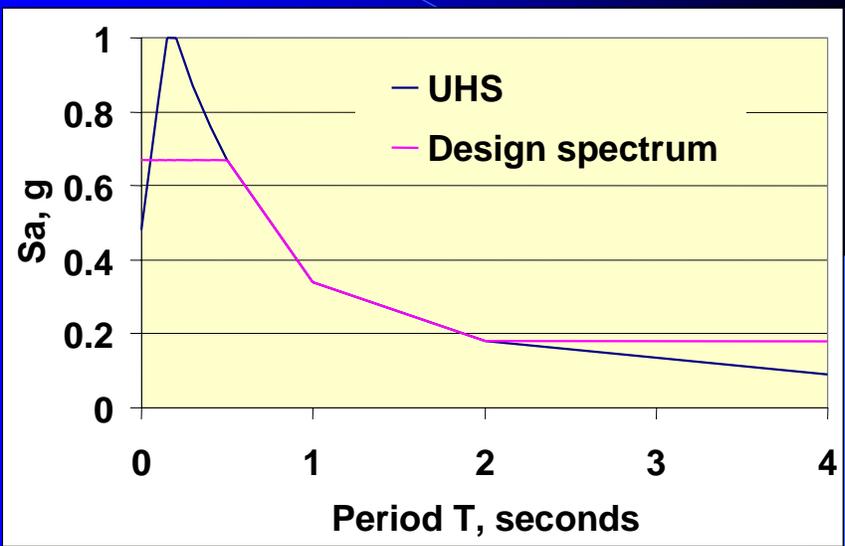
2%/50 year UHS, firm ground  
(soil class C), 5% damping



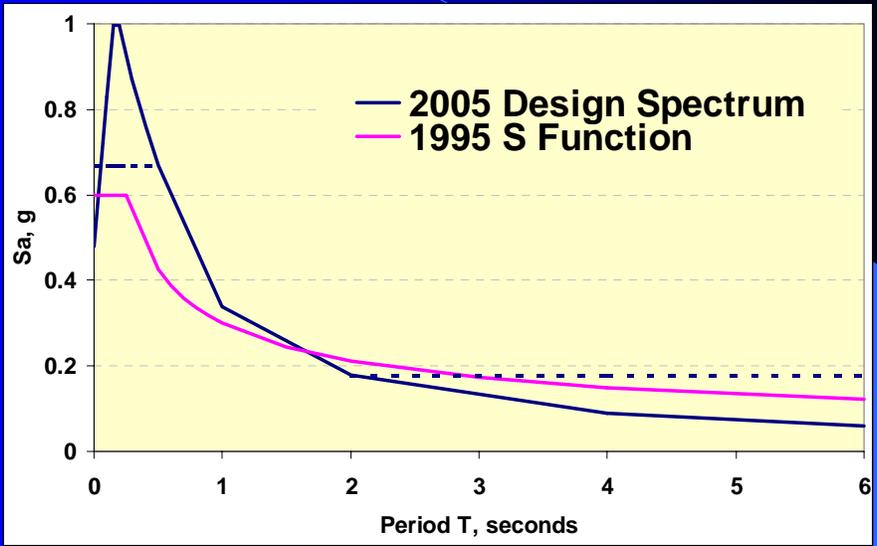
**Representation Of Seismic Hazard  
Uniform Hazard Spectrum**

- Provides maximum acceleration for a 5% damped SDOF system at selected periods,  $S_a(T)$
- Spectral values derived for a uniform probability of exceedance, 2% in 50 years
- Does not include the subduction earthquake

### Vancouver, 2%50 year hazard



### Vancouver NBCC 2005 vs 1995



## Foundation Factor

- Foundation soil generally amplifies wave motion as it propagates up through the layer
- Amplification depends on stiffness and depth of soil, as well as on ground motion intensity
- Foundation factor  $F$  in NBCC 1995 will be replaced by factor  $F_a$  for short periods and  $F_v$  for long periods

## Foundation Site Classification

Site class	Soil profile name	Average properties in top 30 m		
		Soil shear wave average velocity $V_{s,}$ m/s	Standard penetration resistance, $N_{60}$	Soil undrained shear strength, $s_u$ , kPa
A	Hard Rock	> 1500	NA	NA
B	Rock	760 to 1500	NA	NA
C	Very dense Soil and soft Rock	360 to 760	> 50	> 100
D	Stiff Soil	180 to 360	15 to 50	50 to 100
E	Soft Soil	< 180	< 15	< 50
E		Any profile with more than 3m of soil with the following characteristics <ul style="list-style-type: none"> <li>• Plastic index <math>PI \geq 20</math></li> <li>• Moisture content <math>w \geq 40\%</math>, and</li> <li>• Undrained shear strength <math>s_u &lt; 25</math> kPa</li> </ul>		
F	<sup>(1)</sup> Others			

<sup>(1)</sup> Other soils include:

- Liquefiable soils, quick and highly sensitive clays, collapsible weakly cemented soils, and other soils susceptible to failure or collapse under seismic loading.
- Peat and/or highly organic clays greater than 3m in thickness
- Highly plastic clays ( $PI > 75$ ) with thickness greater than 8m
- Soft to medium stiff clays with thickness greater than 30m

<b>F<sub>a</sub></b>					
Site Class	<b>S<sub>a</sub>(0.2)</b>				
	<b>≤ 0.25</b>	<b>0.50</b>	<b>0.75</b>	<b>1.00</b>	<b>1.25</b>
A	0.7	0.7	0.8	0.8	0.8
B	0.8	0.8	0.9	1.0	1.0
C	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>
D	1.3	1.2	1.1	1.1	1.0
E	2.1	1.4	1.1	0.9	0.9
F	Site specific geotechnical investigation and dynamic site response required				

<b>F<sub>v</sub></b>					
Site Class	<b>S<sub>a</sub>(1.0)</b>				
	<b>≤ 0.10</b>	<b>0.20</b>	<b>0.30</b>	<b>0.40</b>	<b>≥ 0.50</b>
A	0.5	0.5	0.5	0.6	0.6
B	0.6	0.7	0.7	0.8	0.8
C	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>
D	1.4	1.3	1.2	1.1	1.1
E	2.1	2.0	1.9	1.7	1.7
F	Site specific geotechnical investigation and dynamic site response required				

## Design Spectral Acceleration

$$S(T) = F_a S_a(0.2) \text{ for } T \leq 0.2 \text{ s}$$

$$= F_v S_a(0.5) \text{ or } F_a S_a(0.2)$$

whichever is smaller,

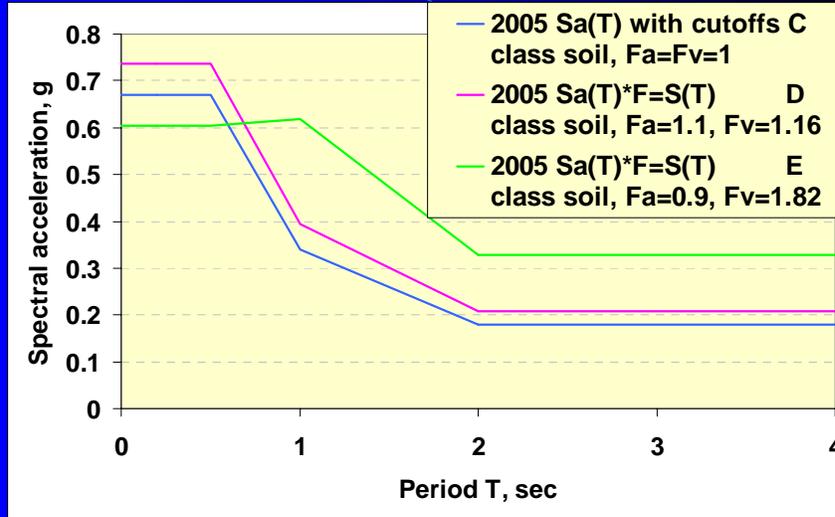
$$\text{for } T = 0.5 \text{ s}$$

$$= F_v S_a(1.0) \text{ for } T = 1.0 \text{ s}$$

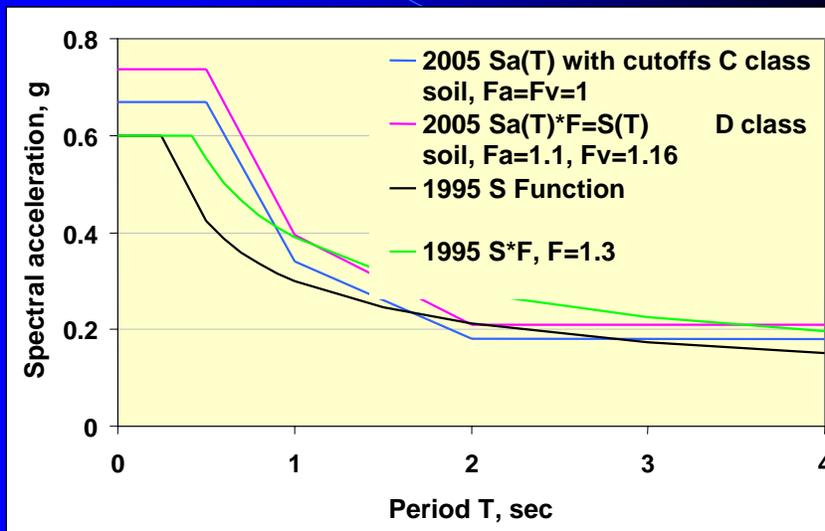
$$= F_v S_a(2.0) \text{ for } T = 2.0 \text{ s}$$

$$= F_v S_a(2.0)/2 \text{ for } T \geq 4.0 \text{ s}$$

## Vancouver NBCC 2005



## Vancouver



## Obtaining Design Forces from UHS

- Dynamic analysis procedure (default method)
- Equivalent static load procedure (allowed for some structures)

## Conditions under which Static Load Procedure may be used

- Structures located in zones of low seismicity, that is,  $I F_a S_a(0.2) < 0.35$ , or
- Regular structures that are less than 60 m in height and have  $T_a < 2$  s, where  $T_a$  is the fundamental period, or
- Irregular structures that are less than 20 m in height, have  $T_a < 0.5$  s and are not torsionally sensitive

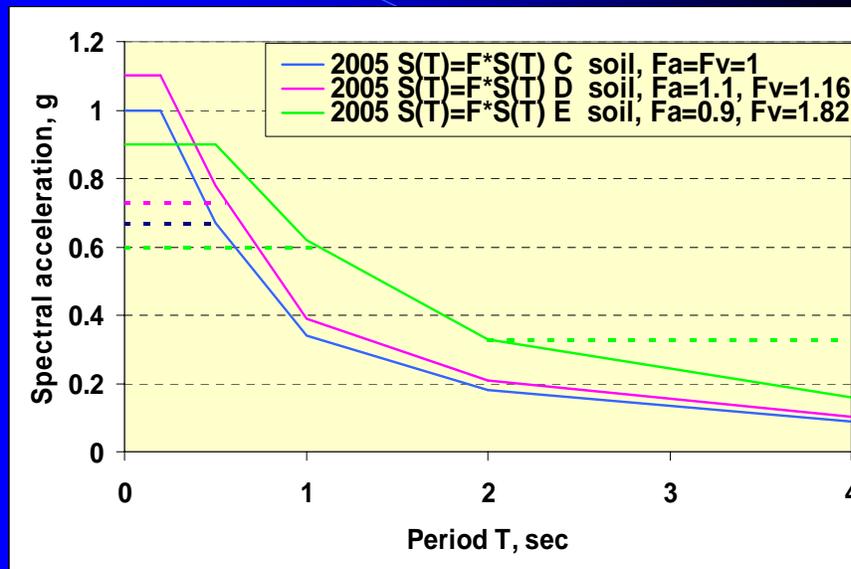
## Equivalent Static Load Procedure Elastic Base Shear

- Elastic base shear is derived from

$$V_e = S(T_a)M_V W, \quad \text{where}$$

- $T_a$  is the fundamental period,
- $W$  is the weight of the structure contributing to inertia forces, and
- $M_V$  is a factor to account for higher mode shears

## Vancouver NBCC 2005 S (T)



## Equivalent Static Load procedure Design Base Shear

$$V = V_e I / R_d R_o$$

$V$  = factored design base shear

$I$  = importance factor, 1.0, 1.3, or 1.5

$R_d$  = ductility related force modification factor

$R_o$  = overstrength related force modification factor

## Equivalent Static Load Procedure Design Base Shear

- Because of uncertainty associated with the  $S_a$  values for periods greater than 2.0 s,  $S(T_a)$  is taken as  $S(2.0)$  for  $T_a > 2.0$
- For ductile structures where  $R_d$  is 1.5 or more, the following upper limit is specified on the design shear (affects short periods)

$$V = \frac{2}{3} \frac{S(0.2)IW}{R_d R_o}$$

## Importance Factor

- $I = 1.3$  Buildings used as post disaster shelters, such as, schools and community centres, and manufacturing facilities containing toxic, explosive or hazardous substances
- $I = 1.5$  Buildings used for post-disaster recovery, such as, hospitals, telephone exchanges, generating stations, fire and police stations, water and sewage treatment facilities
- $I = 1.0$  All other buildings

## Fundamental Period $T_a$

Calculation of period by analytical methods allowed, but the value should be limited to a multiple of the empirical value; 1.5 for moment frames, 2.0 for braced frames and shear walls. Reasons are:

- Possible inaccuracies in modelling
- Difference between design and as-built condition
- Uncertainties regarding participation of non-structural elements

## Fundamental Period Empirical Expressions

For concrete frames

$$T = 0.075 (h_n)^{3/4}$$

For steel frames

$$T = 0.085 (h_n)^{3/4}$$

For other moment frames

$$T = 0.1N$$

where  $h_n$  is the height above base in m and  $N$  is the total number of storeys above grade

## Fundamental Period Empirical Expressions

Braced frames  $T = 0.025 h_n$

Shear wall buildings  $T = 0.05 (h_n)^{3/4}$

The corresponding NBCC 1995 formula was

$$T = \frac{0.09 h_n}{\sqrt{D_s}}$$

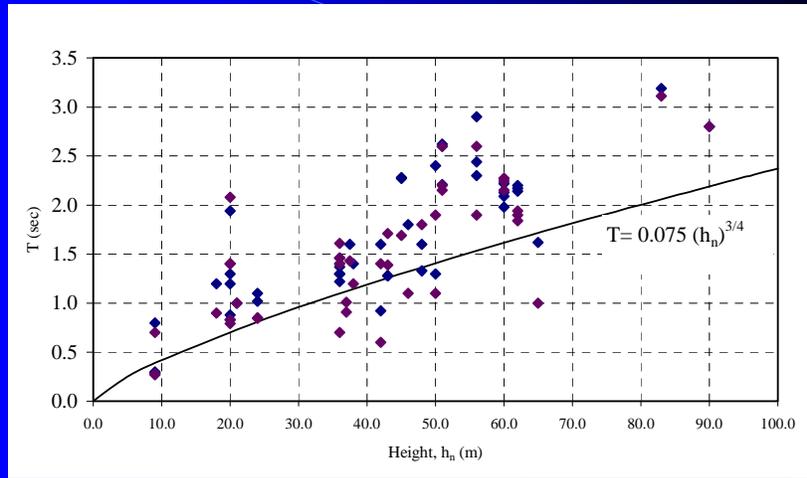


Fig. 2: Comparison of empirical and measured periods for concrete moment frame buildings

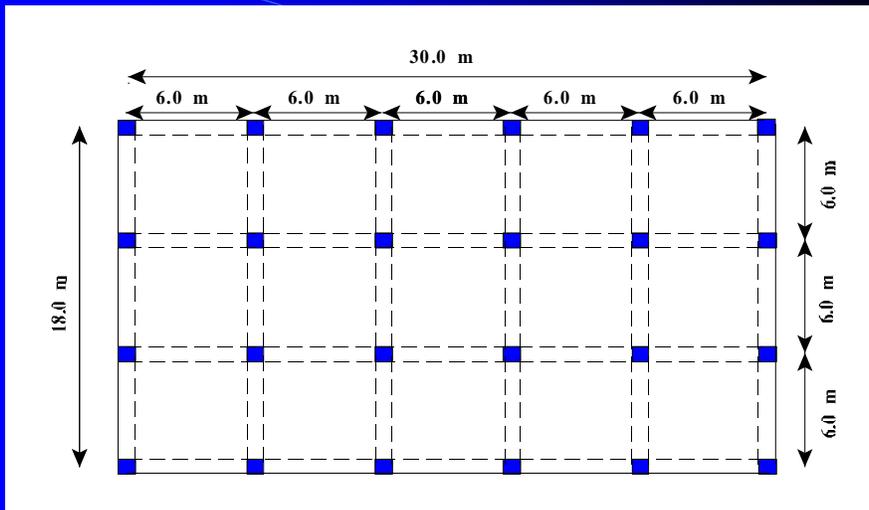


Fig. 3a: Concrete frame buildings, plan

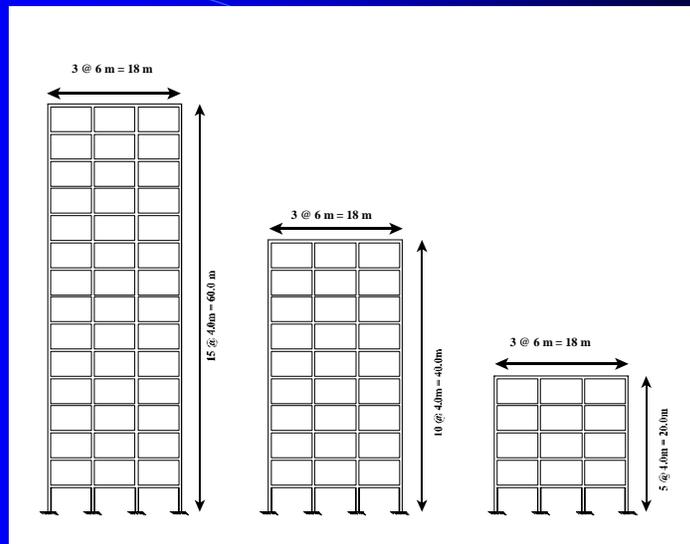


Fig. 3b: Concrete frame buildings, Elevations

## Empirical Versus Analytical Periods

Building height	NBCC period s	Analytical period s
5	0.7	1.7
10	1.2	3.7
15	1.6	5.7

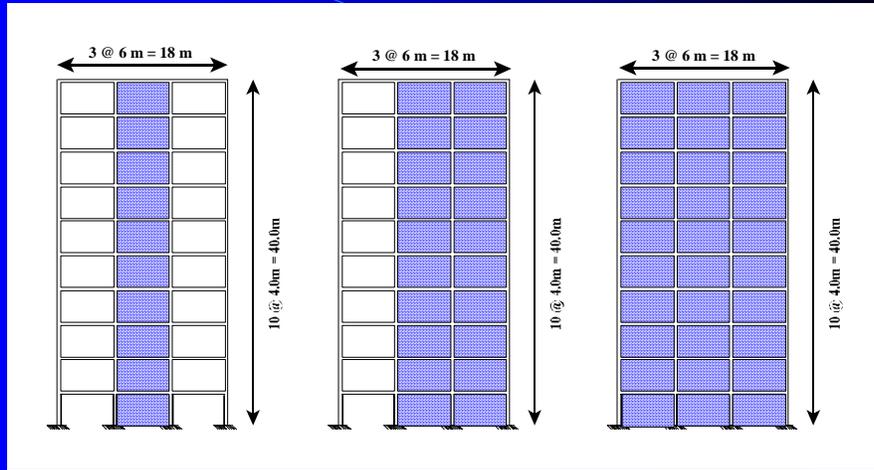


Fig. 4: masonry infill walls in exterior frames

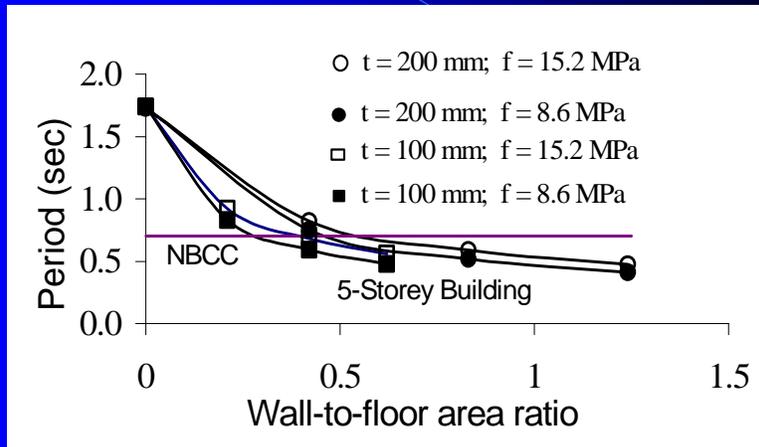


Fig. 5: Effect of masonry infills, 5-storey building

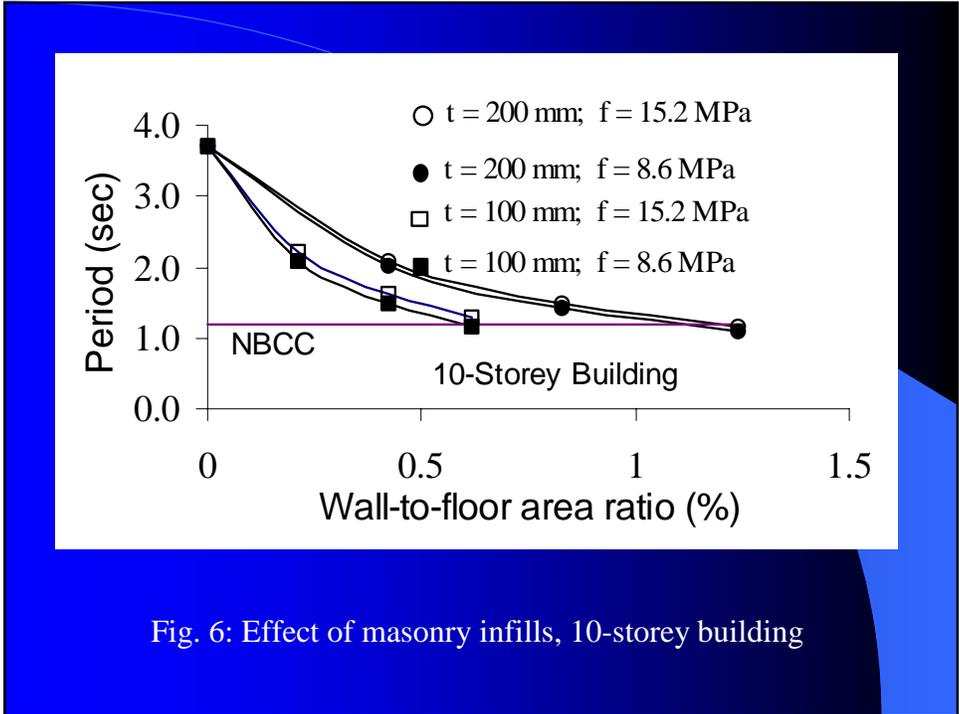


Fig. 6: Effect of masonry infills, 10-storey building

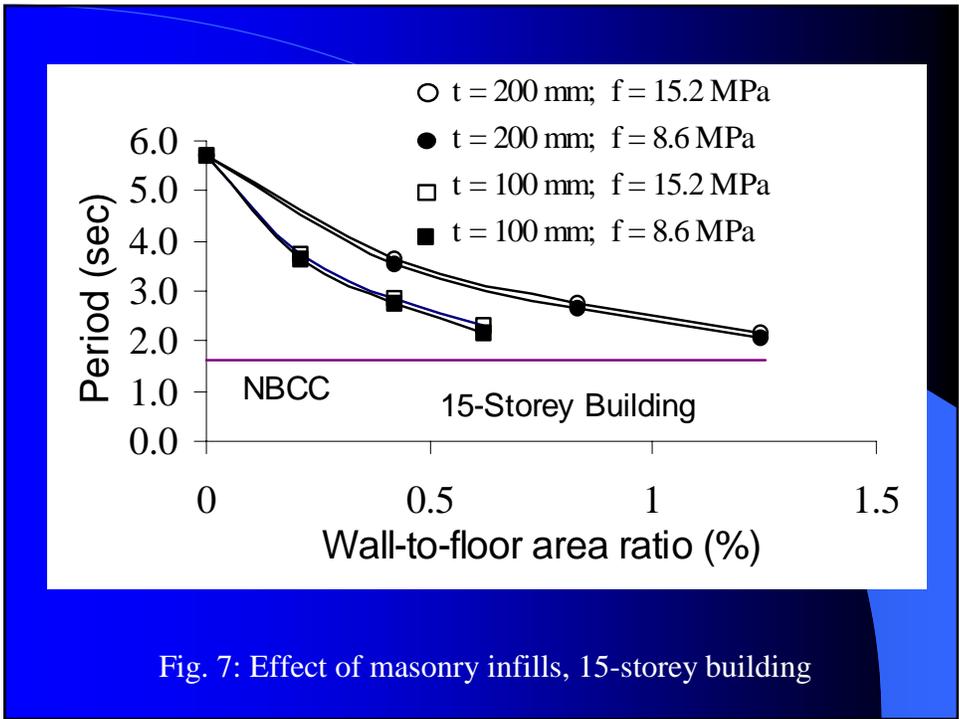


Fig. 7: Effect of masonry infills, 15-storey building

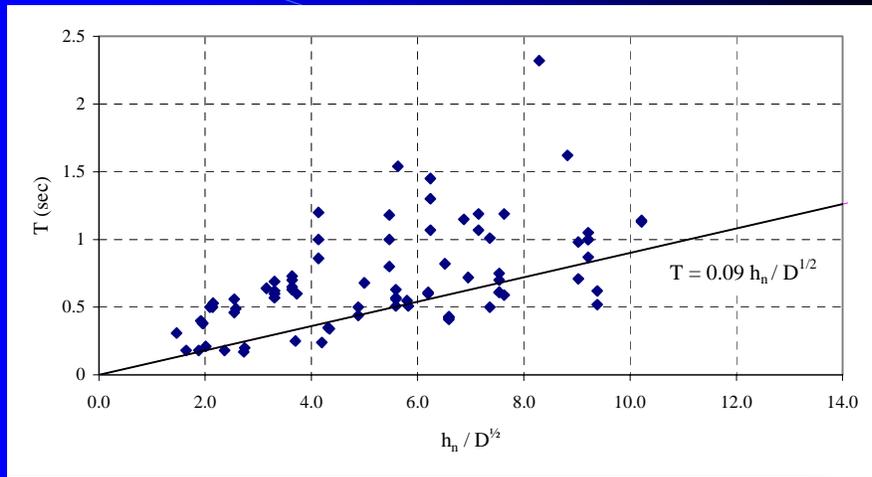


Fig. 8: Comparison of empirical and measured periods, concrete shear wall buildings, 1995 code period formula.

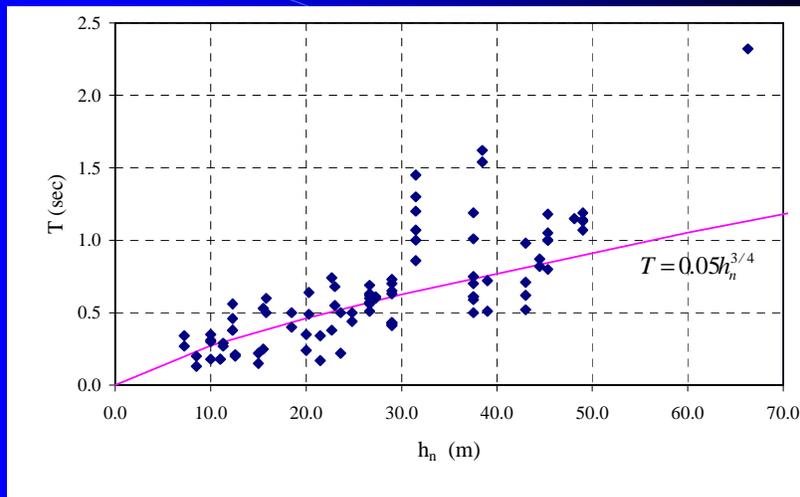


Fig. 9: Comparison of empirical and measured periods, concrete shear wall buildings, 2005 code period formula.

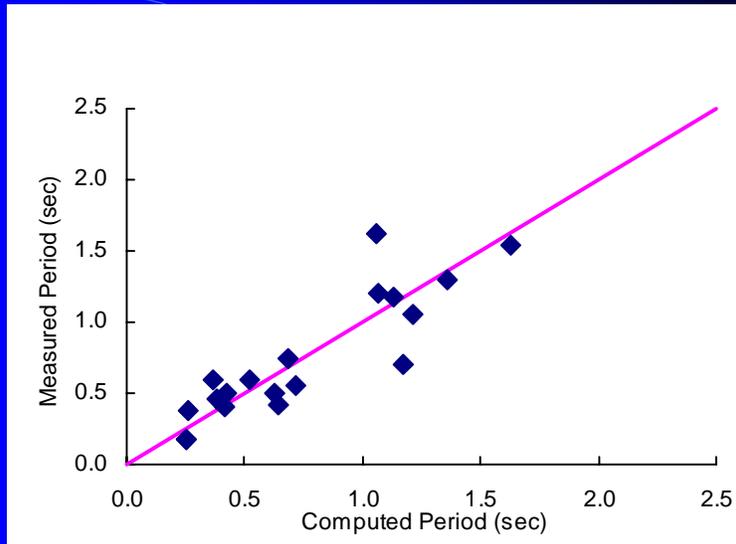


Fig. 10: Comparison of analytical and measured periods, concrete shear wall buildings

## Equivalent Static Load Procedure Elastic Base Shear

- Elastic base shear is derived from

$$V_e = S(T_a)M_V W, \quad \text{where}$$

$T_a$  is the fundamental period,

$W$  is the weight of the structure contributing to inertia forces, and

- $M_V$  is a factor to account for higher mode shears

## Effect of Higher Modes on Base Shear, $M_v$ factor

Relative contribution of higher modes depends on

1. Spectral shape
2. Relative modal periods
3. Mass participation factor

**Table 3:** Proposed base shear and overturning moment adjustment factors,  $M_v$  and  $J$  for different structural systems <sup>(1,2)</sup>

$\frac{S_a(0.2)}{S_a(2.0)}$	Type of lateral force resisting system	$M_v$ for $T \leq 1.0$	$M_v$ for $T \geq 2.0$	$J$ for $T \leq 0.5$	$J$ for $T \geq 2.0$
< 8.0	Moment-resisting frames or "coupled walls" <sup>(3)</sup>	1.0	1.0	1.0	1.0
	Braced frames	1.0	1.0	1.0	0.8
WEST	Walls, wall-frame systems, other systems <sup>(4)</sup>	1.0	1.2	1.0	0.7
> 8.0	Moment-resisting frames or "coupled walls" <sup>(3)</sup>	1.0	1.2	1.0	0.7
	Braced frames	1.0	1.5	1.0	0.5
EAST	Walls, wall-frame systems, other systems <sup>(4)</sup>	1.0	2.5	1.0	0.4

Notes:

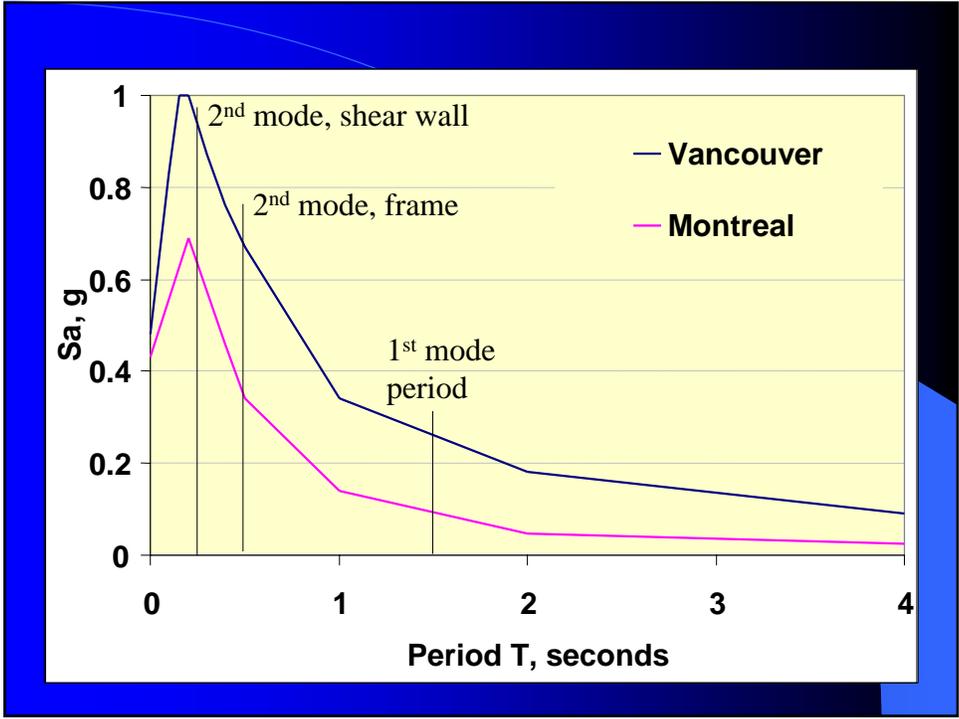
1. Values of  $M_v$  between periods of 1.0 and 2.0 s are to be obtained by linear interpolation.
2. Values of  $J$  between periods of 0.5 and 2.0 s are to be obtained by linear interpolation.
3. Coupled wall is a wall system with coupling beams where at least 66% of the base overturning moment resisted by the wall system is carried by axial tension and compression forces resulting from shear in the coupling beams
4. For hybrid systems, use values corresponding to walls or carry out a dynamic analysis

Relative modal periods and modal weights for flexural and shear cantilevers

Mode No.	Uniform shear wall		Uniform frame, stiff beams	
	Period	Modal weight	Period	Modal weight
1	1.000	0.616	1.000	0.811
2	0.167	0.188	0.333	0.090
3	0.057	0.065	0.200	0.032
4	0.030	0.032	0.143	0.017
5	0.018	0.020	0.111	0.010

## Effect of Higher Modes on Base Shear - example

- Consider a building structure with first mode period of 1.5 s
- Assume that contribution from only the first two modes are significant
- Use the UHS for Vancouver and Montreal and the data in previous table



**Design shears in a building of two different structural types located in Vancouver and Montreal**

Structure type	1 <sup>st</sup> mode period	2 <sup>nd</sup> mode period	Modal weight in 1 <sup>st</sup> mode	Modal weight in 2 <sup>nd</sup> mode	Spectral acceleration (g) in 1 <sup>st</sup> mode	Spectral acceleration (g) in 2 <sup>nd</sup> mode	Base shear in 1 <sup>st</sup> mode	Base shear in 2 <sup>nd</sup> mode	SRSS shear	Base shear assuming entire weight at 1 <sup>st</sup> mode period	$M_y$
Vancouver											
Frame	1.50	0.50	0.811W	0.090W	0.256	0.630	0.208W	0.057W	0.216W	0.256W	0.84
Shear wall	1.50	0.25	0.616W	0.188W	0.256	0.900	0.158W	0.169W	0.231W	0.256W	0.90
Montreal											
Frame	1.50	0.50	0.811W	0.090W	0.073	0.340	0.059W	0.031W	0.067W	0.073W	0.91
Shear wall	1.50	0.25	0.616W	0.188W	0.073	0.600	0.045W	0.113W	0.122W	0.073W	1.67

## Methodology for Estimating Shear Adjustment Factor

$$M_v = \frac{\sqrt{\sum \{S_a(T_i)W_i\}^2}}{S_a(T_1)W} = \frac{V_b}{S_a(T_1)W}$$

$S_a(T_i)$  = spectral acceleration in the  $i$  th mode

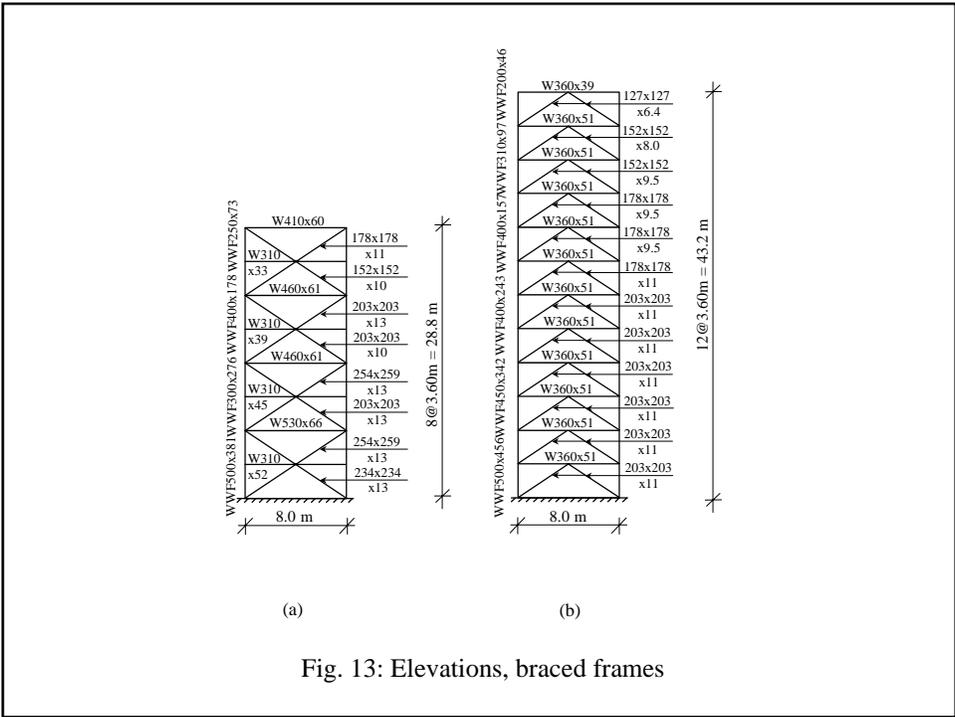
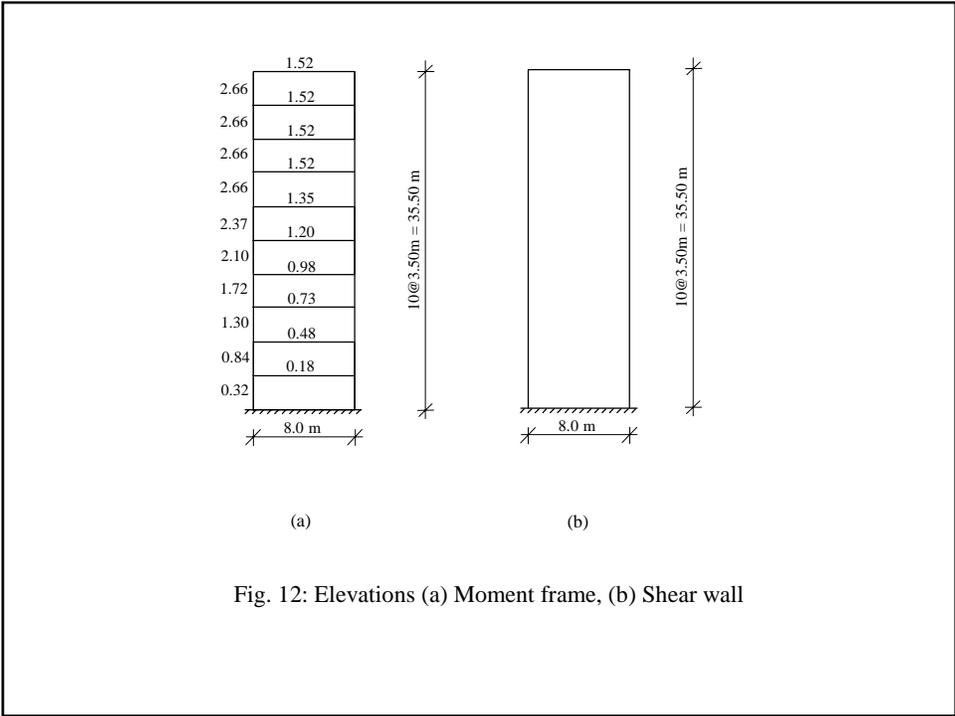
$T_i$  =  $i$  th mode period

$W_i$  = modal weight in the  $i$  th mode

## Shear Adjustment Factor $M_v$

Structural types studied

1. Moment-resisting frame
2. Centrically braced frame
3. Flexural wall
4. Coupled flexural walls
5. Hybrid frame-wall system



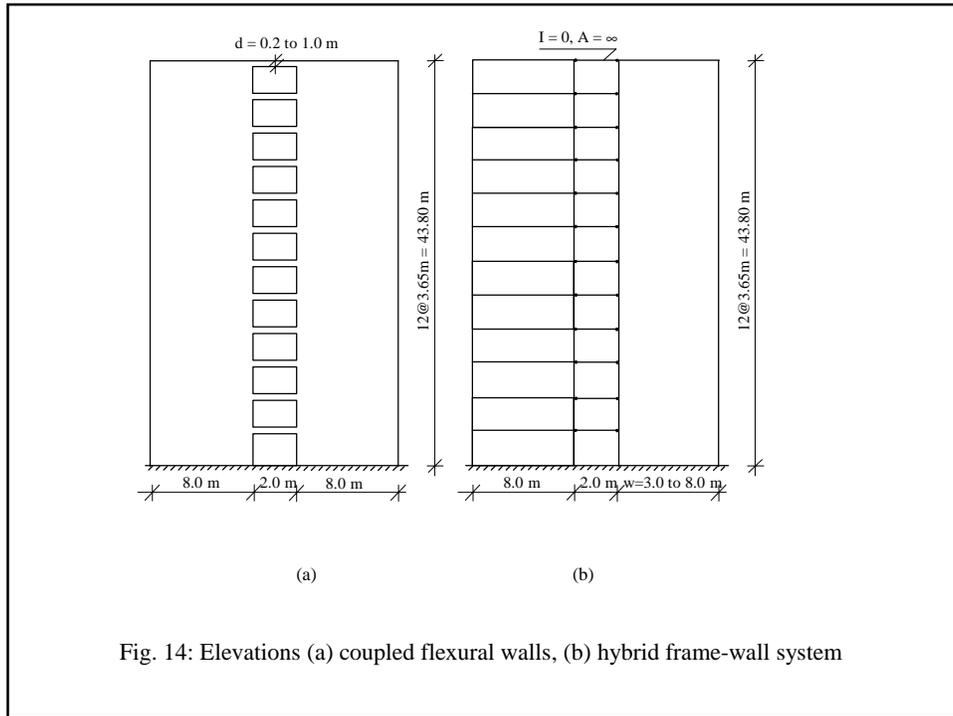


Fig. 14: Elevations (a) coupled flexural walls, (b) hybrid frame-wall system

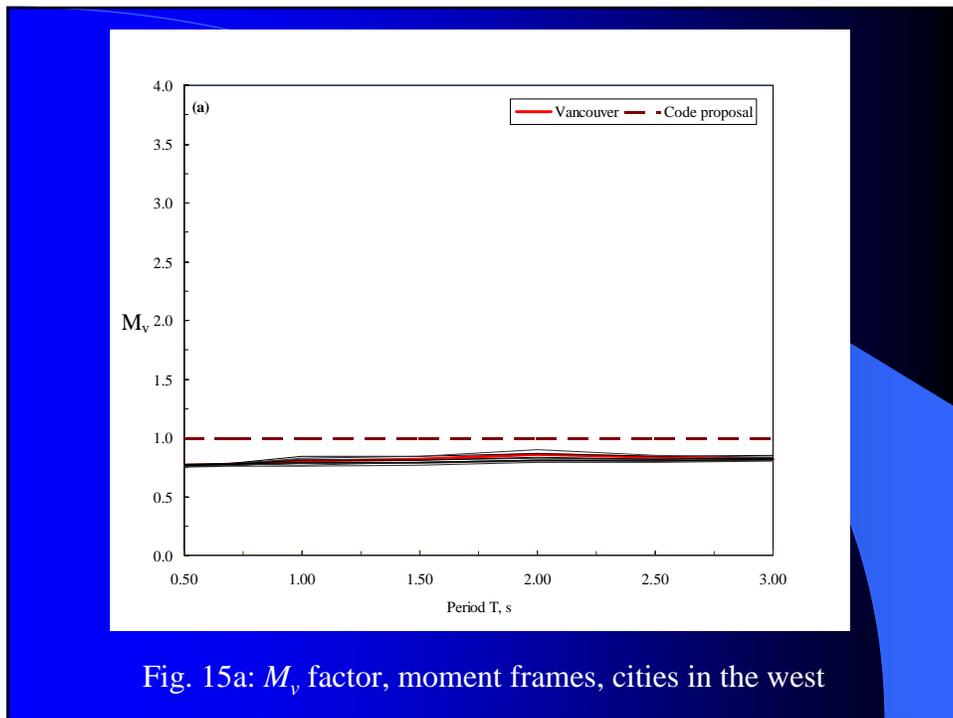


Fig. 15a:  $M_v$  factor, moment frames, cities in the west

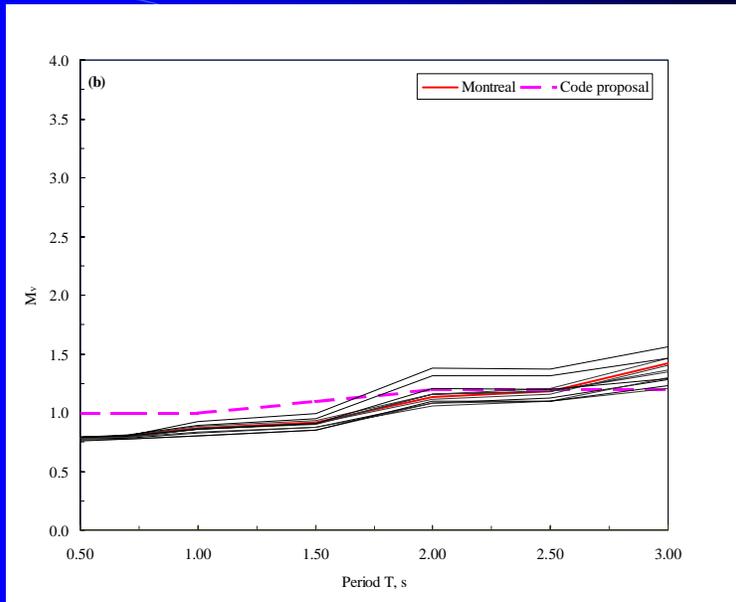


Fig. 15b:  $M_v$  factor, moment frames, cities in the east

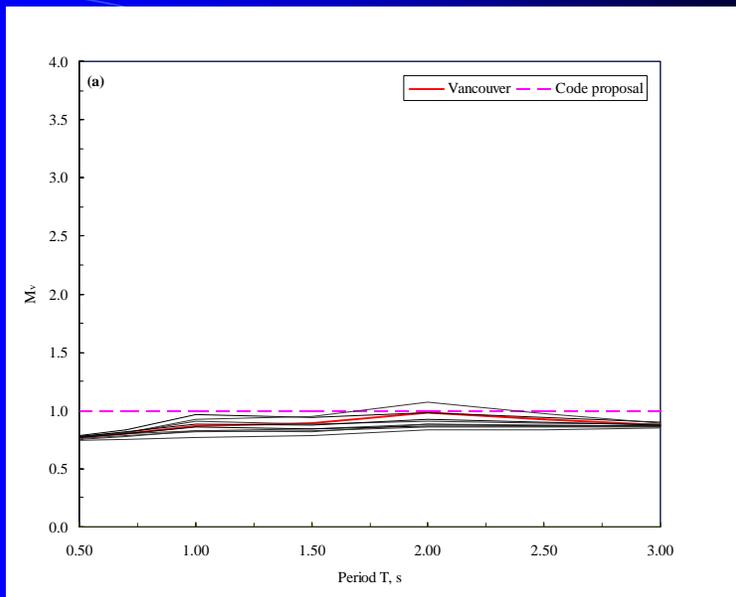


Fig. 16a:  $M_v$  factor, braced frames, cities in the west

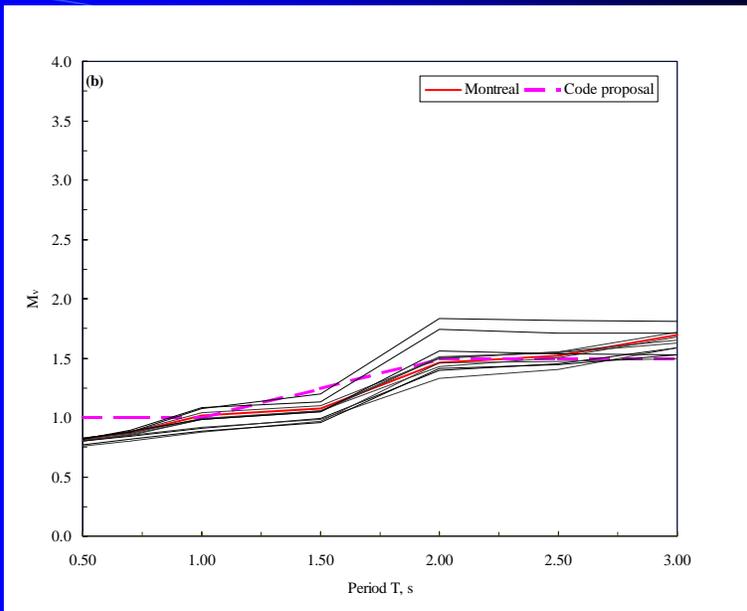


Fig. 16b:  $M_v$  factor, braced frames, cities in the east

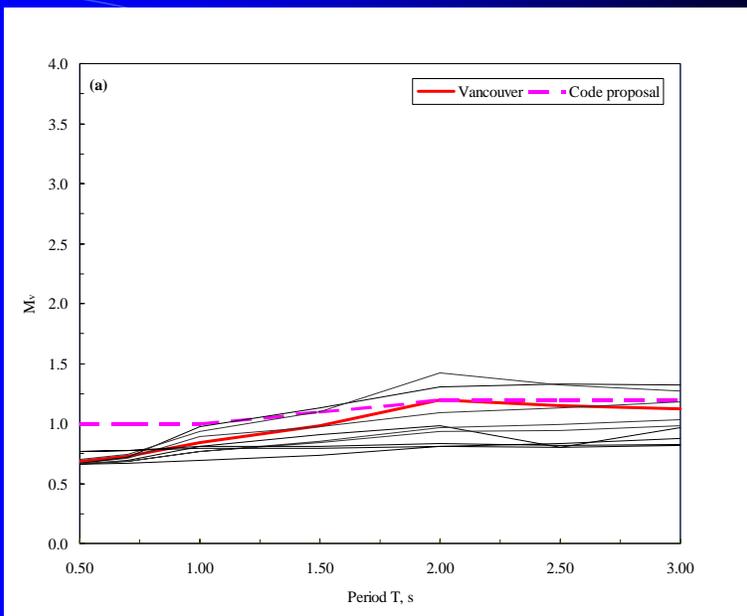


Fig. 17a:  $M_v$  factor, shear walls, cities in the west

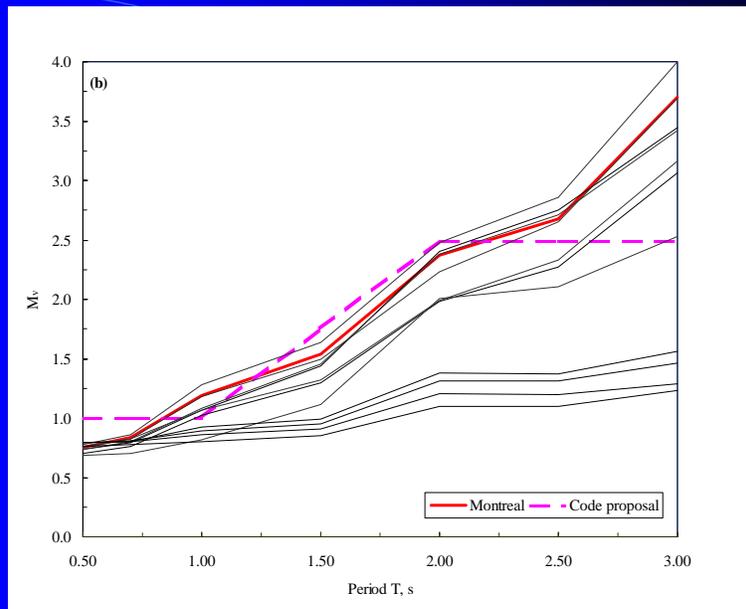


Fig. 17b:  $M_v$  factor, shear walls, cities in the east

## Distribution of Shear

Similar expressions are used in NBCC 1995 and NBCC 2005

$$F_i = \frac{W_i h_i}{\sum W_i h_i} (V - F_t)$$

$$\begin{aligned}
 F_t &= 0 & \text{for } T_a &\leq 0.7 \\
 F_t &= 0.07T_a V & \text{for } 0.7 < T_a < 3.6 \\
 F_t &= 0.25V & \text{for } T_a &\geq 3.6
 \end{aligned}$$

## Overtuning Moments

- Estimates of overturning moment depend on the manner in which the base shear is distributed up the height
- First mode distribution gives the highest overturning moments
- Higher mode effects are important near the top of the structure

## Moment Adjustment Factor $J$

- NBCC distribution is based predominantly on first mode, except for  $F_t$  applied at top
- An adjustment factor  $J$  is applied to the base overturning moment to account for higher mode effects (and  $F_t$ )
- Adjustment factor  $J_x$  is applied to the calculated moment at level  $x$

## Determination of J, J<sub>x</sub> factor

1. Determine from the code static shear forces the overturning moment at the base,  $M_{bc}$ , and at each level  $x$ ,  $M_{xc}$ .
2. Obtain more precise estimates of the base moment,  $M_{bd}$ , and at each level,  $M_{xd}$ , by a dynamic response spectrum analysis
3. Then,  $J = M_{bd}/M_{bc}$ ,  $J_x = M_{xd}/M_{xc}$

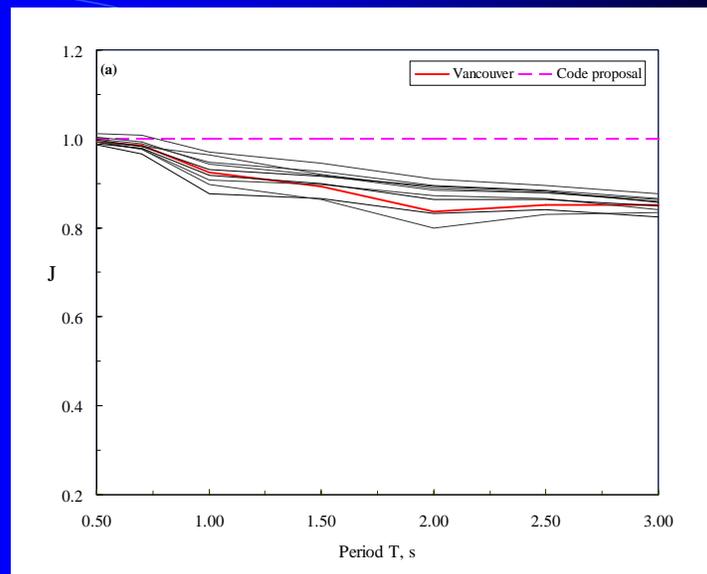


Fig. 18a: J factor, moment frames, cities in the west

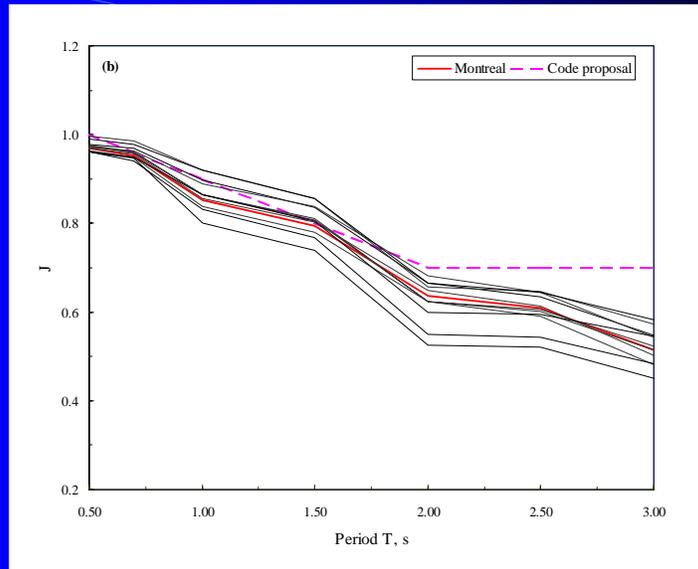


Fig. 18b:  $J$  factor, moment frames, cities in the east

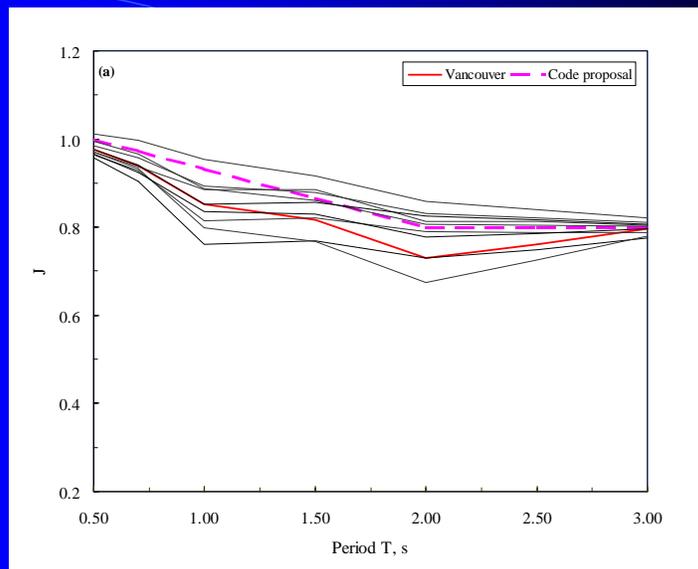


Fig. 19a:  $J$  factor, braced frames, cities in the west

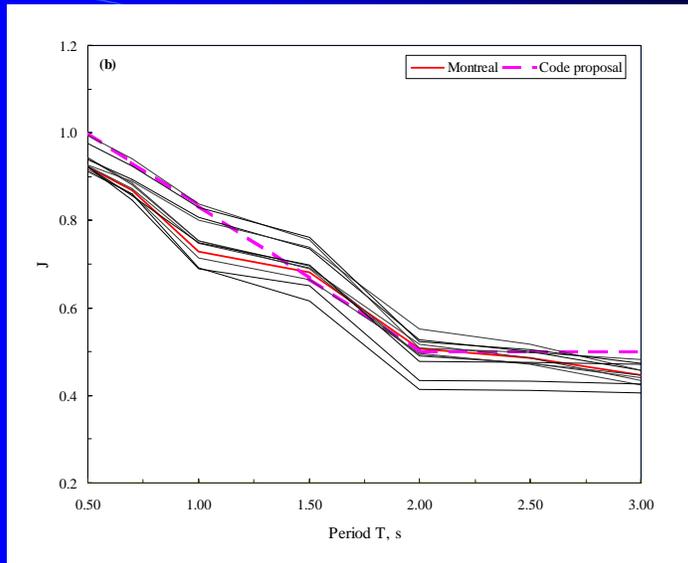


Fig. 19b:  $J$  factor, braced frames, cities in the east

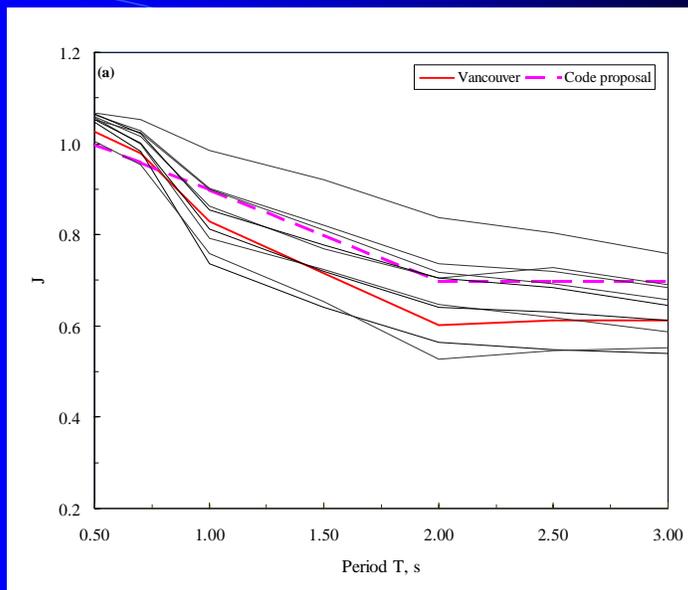


Fig. 20a:  $J$  factor, shear walls, cities in the west

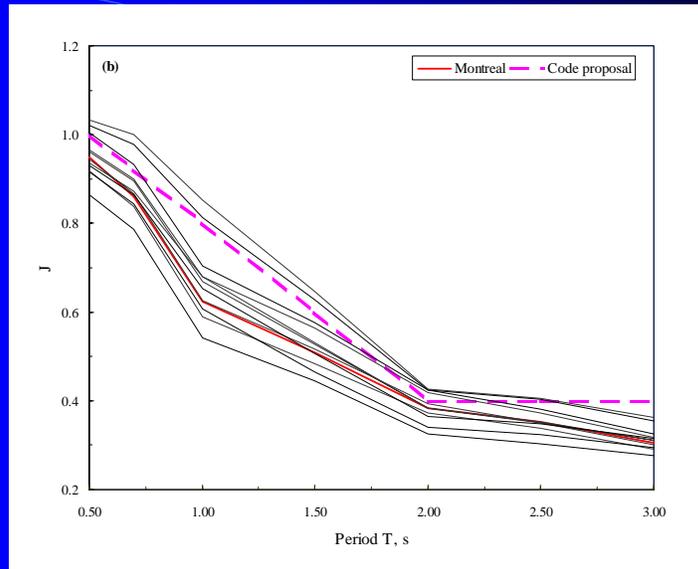


Fig. 20b:  $J$  factor, shear walls, cities in the east

Proposed base shear and overturning moment adjustment factors,  $M_v$  and  $J$  for different structural systems<sup>(1,2)</sup>

$\frac{S_a(0.2)}{S_a(2.0)}$	Type of lateral force resisting system	$M_v$		$J$	
		$T \leq 1.0$	$T \geq 2.0$	$T \leq 0.5$	$T \geq 2.0$
< 8.0	Moment-resisting frames or "coupled walls" <sup>(3)</sup>	1.0	1.0	1.0	1.0
	Braced frames	1.0	1.0	1.0	0.8
WEST	Walls, wall-frame systems, other systems <sup>(4)</sup>	1.0	1.2	1.0	0.7
	Moment-resisting frames or "coupled walls" <sup>(3)</sup>	1.0	1.2	1.0	0.7
>8.0	Braced frames	1.0	1.5	1.0	0.5
	EAST Walls, wall-frame systems, other systems <sup>(4)</sup>	1.0	2.5	1.0	0.4

Notes:

1. Values of  $M_v$  between periods of 1.0 and 2.0 s are to be obtained by linear interpolation.
2. Values of  $J$  between periods of 0.5 and 2.0 s are to be obtained by linear interpolation.
3. Coupled wall is a wall system with coupling beams where at least 66% of the base overturning moment resisted by the wall system is carried by axial tension and compression forces resulting from shear in the coupling beams
4. For hybrid systems, use values corresponding to walls or carry out a dynamic analysis

## Overtuning Moment Reduction Factor, $J_x$

$$J_x = 1.0 \quad \text{for } h_x \geq 0.6h_n$$

$$J_x = J + (1 - J) \frac{h_x}{h_n} \quad \text{for } h_x < 0.6h_n$$

i.e.,  $J_x = 1$  for top 40% of the building, then reduces linearly to  $J_x = J$  at the base of the building.

## Provisions for Torsion Design

NBCC 1995 design eccentricities

$$e_{d1} = 1.5e + 0.1b$$

$$e_{d2} = 0.5e - 0.1b$$

NBCC 2005 design eccentricities

$$e_{d1} = e + 0.1b$$

$$e_{d2} = e - 0.1b$$

- $0.05b$  is considered adequate to account for accidental torsion
- The remaining  $0.05b$  should take care of the amplification of the natural torsion
- The  $0.1b$  accidental torsion can be applied dynamically by shifting the mass by  $\pm 0.05b$  if the structure is ‘torsionally stiff’ ( $B \leq 1.7$ ), else it must be applied statically

## Forces Induced by Seismic Torsion

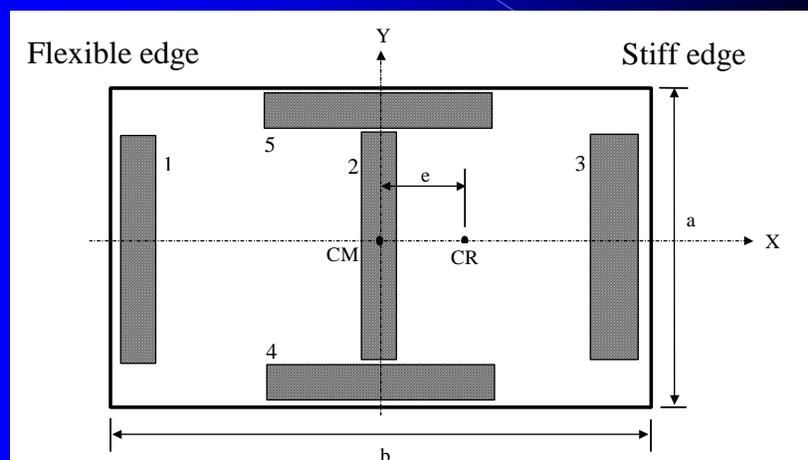


Fig. 22: Torsionally unbalanced building

## Torsion Related Parameters

$e$  = eccentricity between CR and CM

$K_y$  = lateral stiffness in y direction

$K_{\theta R}$  = torsional stiffness about CR

$\omega_y = \sqrt{\frac{K_y}{m}}$  = uncoupled lateral frequency

$\omega_\theta = \sqrt{\frac{K_{\theta R}}{mr^2}}$  = uncoupled torsional frequency

$\Omega_R = \frac{\omega_\theta}{\omega_y}$  = frequency ratio

Large  $\Omega_R$  = torsionally stiff building

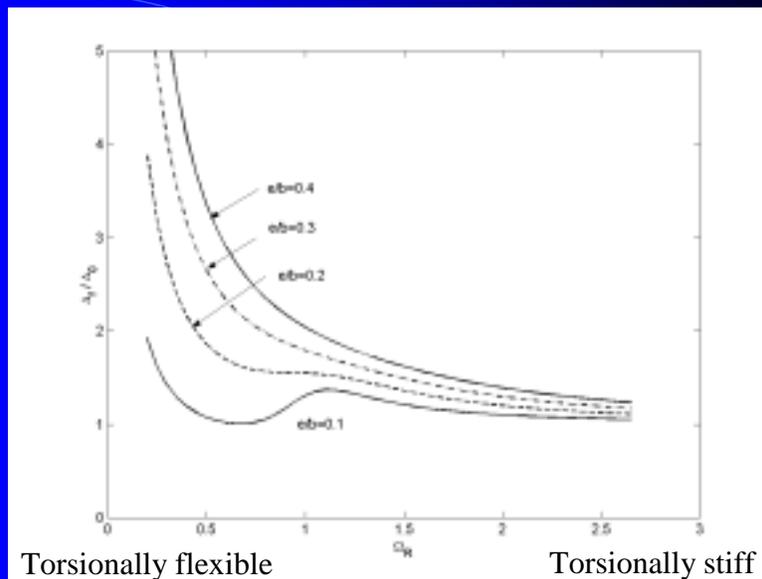


Fig. 23: Flexible edge displacement, hyperbolic spectrum, aspect ratio = 1

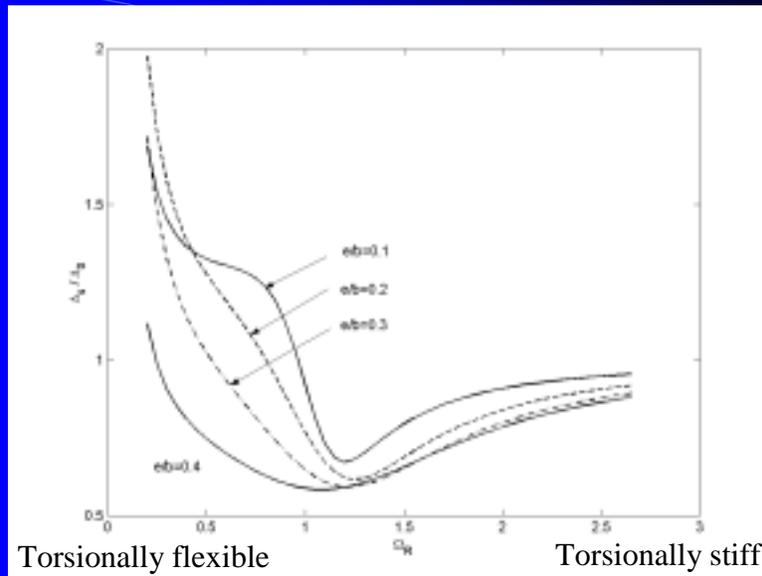


Fig. 24: Stiff edge displacement, hyperbolic spectrum, aspect ratio = 1

## NBCC 2005 Provisions for Torsion

Use dynamic analysis for  $B > 1.7$ , where

$B$  is the largest value of  $B_x$ , where

$$B_x = \delta_{\max} / \delta_{\text{ave}}$$

$\delta_{\max}$  = maximum displacement at extreme points of storey  $x$ , produced by lateral forces applied at an eccentricity of  $\pm 0.1b_{nx}$

$\delta_{\text{ave}}$  = average of the displacements at extreme points of storey  $x$  produced by the lateral forces

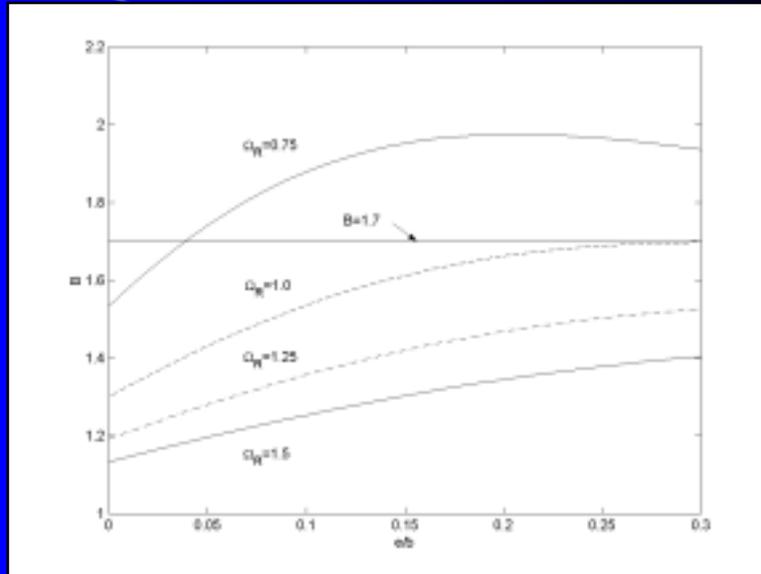


Fig. 27: Variation of torsional sensitivity parameter  $B$

## Deflections and Drift Limits

- Deflections calculated from an elastic analysis for the design forces shall be multiplied by  $R_d R_o / I$  to give the design deflections
- For any storey deflections should be limited to  $0.01 h_s$  for post-disaster buildings,  $0.02 h_s$  for schools, and  $0.025 h_s$  for all other buildings, where  $h_s$  is the storey height

## Dynamic Analysis

Dynamic analysis required for the following class of buildings

- Regular structures that have  $h \geq 60$  m, or have  $T_a \geq 2$  s, and are located in areas in which  $IF_a S_a(0.2) \geq 0.35$
- Irregular buildings that have  $h \geq 20$  m, or have  $T_a \geq 0.5$  s, and are located in areas in which  $IF_a S_a(0.2) \geq 0.35$
- All buildings that have rigid diaphragms and are torsionally sensitive, i.e.  $B \geq 1.7$

## Scaling of Dynamic Analysis

- Obtain the dynamic elastic base shear  $V_e$
- Obtain dynamic design base shear  $V_d = V_e I / R_d R_o$
- If  $V_d < 0.8V_{static}$ , take  $V_d$  to be no less than  $0.8V_{static}$
- For irregular structures requiring dynamic analysis  $V_d$  should be taken no less than  $V_{static}$

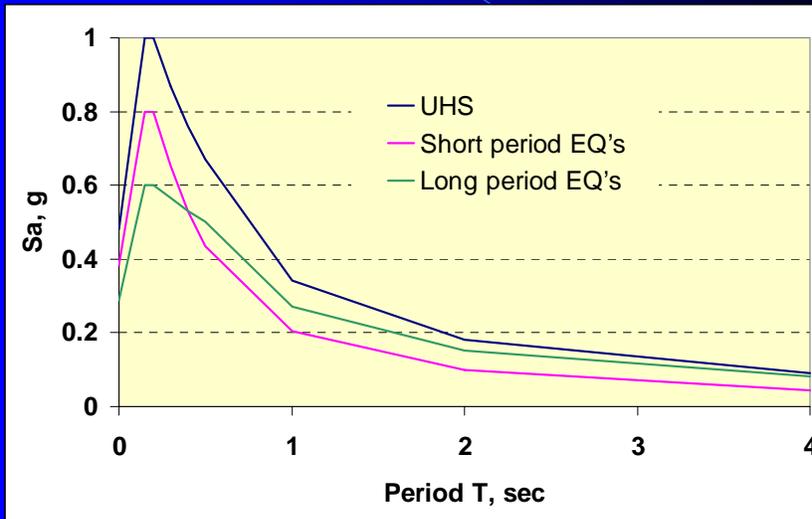
## Dynamic Analysis Methods

- Modal response spectrum method – linear, expected to be most common dynamic method used
- Numerical integration linear time history method
- Numerical integration nonlinear time history method

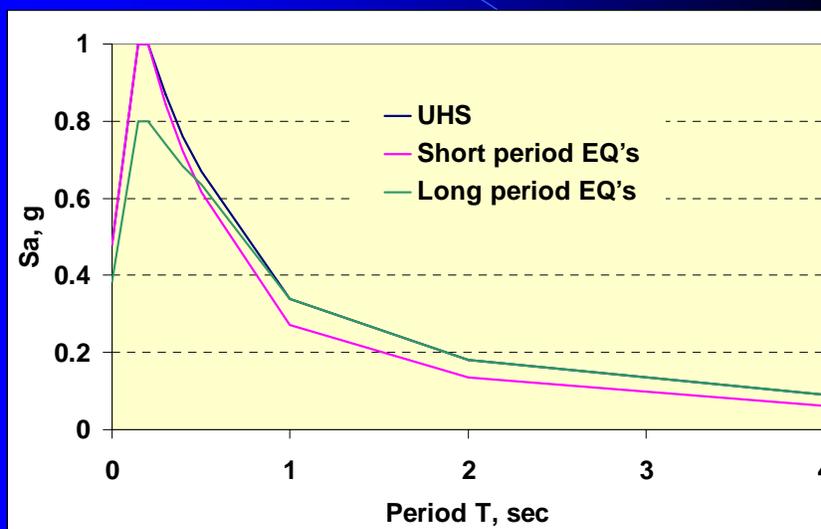
## Response spectrum

- A response spectrum provides the maximum response of a SDOF system, for a given damping ratio and a range of periods, for a specific earthquake
- A design response spectrum is a smoothed spectrum used to calculate the expected seismic response of a structure
- A Uniform Hazard Spectrum (UHS) is a spectrum, for a given damping ratio, that has equal probability of occurring at all periods

## Schematic of contribution to UHS of different type earthquakes



## Two Spectrum Analysis Representation of UHS



## Use of UHS in Modal Analysis

- Use of UHS in modal analysis will provide conservative results
- A number of calculations show the overestimation of response to be not more than 10%

## Dynamic Analysis Methods

- Modal response spectrum method - linear
- Numerical integration linear time history method
- Numerical integration nonlinear time history method

**Time history analysis requires ground motion records**

## Ground Motion Record Selection

- Ground motion records:
  - Should be of appropriate magnitude and distance
  - Some codes recommend at least 3 records with the maximum response being used, or the use of at least 7 records if the average response is used.
  - Should be scaled to be compatible with the design spectrum

## Ground motion compatibility

Ground motion records should be compatible with the design spectrum

Two methods of making ground motion records compatible with a spectrum

- Scaling of records until the spectrum of the record is close to the design spectrum in the period range of interest – generally the 1<sup>st</sup> and 2<sup>nd</sup> mode periods
- Modifying the records so that the spectrum of the modified record matches the design spectrum

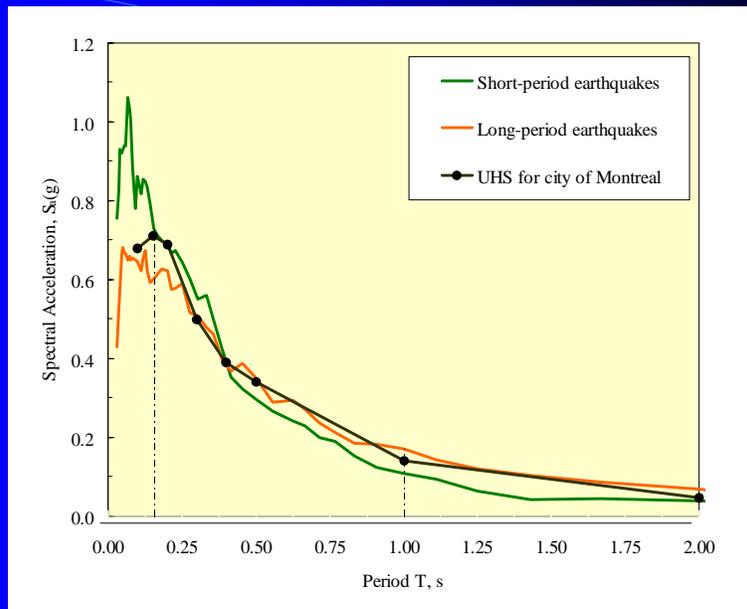


Fig. 11: Spectra for two sets of UHS-compatible records for Montreal

## Ground motion compatibility

Ground motion records should be compatible with the design spectrum

Two methods of making ground motion records compatible with a spectrum

- Scaling of records until the spectrum of the record is close to the design spectrum in the period range of interest – generally the 1<sup>st</sup> and 2<sup>nd</sup> mode periods
- Modifying the records so that the spectrum of the modified record matches the design spectrum

- Records modified to fit the design spectrum
  - There are programs that will modify an acceleration record so that the response spectrum matches the target spectrum
  - There is controversy over the use of modified records but they have two great advantages:
    1. there is not as much scatter in the results, and
    2. not as much care must be taken in selecting the original records

The End